# MATHEMATICS DEPARTMENT <br> COURSE OF STUDY 

## HONORS ALGEBRA II

2010-2011
Course Number: 522

## Prerequisites: Prealgebra, Algebra 1 with Successful Placement Test Results or Honors Algebra 2, and Department Recommendation. <br> Calculators: TI-83, TI-84, or Ti-nspire

## Prerequisites: Prealgebra, Algebra I, Placement Test and/or Department Recommendation

Course Description: This course is designed to provide the student with a thorough treatment of all the major topics of basic algebra. These topics include: the operations and axioms of real numbers; operations with polynomials, exponents, radicals and rationals; the solution and graph of linear quadratic, cubic, and quartic polynomial functions and relations; the solution and graph of exponential, logarithmic, rational and radical functions; the solution and graph of systems of linear and quadratic functions and relations; variation; conics, sequences, series and probability $\&$ an introduction to trigonometry.

## Unit 1: Sets of Numbers and Their Properties

Classes: 5
Project: Create a file box to record significant concept learned.
Create Venn diagram for the sets of numbers.
Nat.Stan: \#1,5,6,7,8,9
Objective 1: The student will be able to demonstrate an understanding of the Real numbers.

## Proficiencies:

1) Display an understanding of Venn diagrams and set notation.
2) Find the union and intersection of sets in a Venn diagram.
3) Know the Venn diagram, which integrates the following sets of numbers:
natural, whole, integers, rational, irrational, transcendental, real, imaginary and complex.
4) Display an understanding of the real number line.

Objective 2: The student will be able to demonstrate an understanding of the axioms and properties of reals.

## Proficiencies:

1) Know and use the axioms, properties and the definitions of reals.
2) Perform basic operations of reals.
3) Know and use the rules for the order of operations.
4) Complete proofs using properties, axioms and definitions.

Objective 3: The student will be able to demonstrate an understanding of the use of algebraic expressions with the reals.

## Proficiencies:

1) Write algebraic expressions from word statements.
2) Substitute and evaluate these expressions using reals.
3) Write and use exponential notation.

Objective 4: The student will demonstrate an understanding of the set of complex numbers and operations with these values.

## Proficiencies:

1) Define the set of imaginary and complex numbers.
2) Recognize a complex number in its monomial and binomial forms.
3) Simplify an imaginary and complex number.
4) Raise an imaginary and complex number to a power.
5) Add, subtract, multiply and divide complex numbers.
6) Graph a complex number on the complex plane.
7) Find the absolute value of a complex number.

## Unit 2: Exponents and their Properties

Classes: 8
Project: Maintain file box of concepts learned.
Tech: Graphing calculator skills: math menu for exponents and use of the following keys: carat, $\mathrm{e}^{\mathrm{x}}$, e, etc.
Nat.Stan: \#1,3,5,6,7,8,9
Objective 1: The student will be able to define and express the concept of an exponent.

## Proficiencies:

1) Define the base, the exponent and the operation of exponentiation.
2) Display an understanding of the use of parenthesis with exponents.
3) Display an understanding of integer and rational exponents.
4) Define and find prime expressions from composite.

Objective 2: The student will be able to operate with exponents.

## Proficiencies:

1) Evaluate using exponentiation.
2) Know and use the properties of exponents for products, quotients, and powers of powers.
3) Use exponents which are negative, zero, fractional, and decimal in form.
4) Know, use and operate in scientific notation.
5) Know and use significant digits.
6) Define the base of e.

## Unit 3: Polynomial and Operations on Polynomials

Classes: 25
Project: $\quad$ Maintain file box of concepts learned.
Tech: Video: Polynomials
Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to display an understanding of the structure of polynomials.

## Proficiencies:

1) Know and use the definition of a polynomial.
2) Write polynomials in ascending and descending order.
3) Give the name and degree of the polynomial.

Objective 2: The student will be able to operate with polynomials.

## Proficiencies:

1) Add and subtract polynomial, i.e., combine like terms.
2) Find products of polynomials.
mono • mono; mono • bin; bin • bin; bin • tri; tri • tri
3) Square a binomial and trinomial and cube a binomial.
4) Perform short and long division with polynomials.
5) Perform synthetic division/substitution.
6) Factor polynomials over the set of complex numbers.

GCF, difference of squares, trinomial squares, quadratic trinomials, difference and sum
of cubes, factor by grouping, negative one technique
7) Know and use the Rational Root Theorem to factor higher degree polynomials.
8) Know and use Descartes' Rule of Signs to determine roots to write the factors of higher degree polynomials.
9) Know and use the sum and product of roots formulas for quadratic expressions.
10) Write the polynomial from its integer, rational, real and complex roots.

## Unit 4: Radicals and their Operations

Classes: 15
Project: Maintain file box on concepts learned.
Nat.Stan: \#1,3,5,6,7,8,9

Objective 1: The student will be able to display an understanding of the concept of radicals.

## Proficiencies:

1) Define radical, radicand, index and root.
2) Convert radical notation too exponential and vice versa.
3) Find the domain of the radical.
4) Relate radicals to the closure property.

Objective 2: The student will be able to perform operations with radicals.

## Proficiencies:

1) Evaluate a radical.
2) Simplify a radical.
3) Add and subtract radicals.
4) Multiply radicals in monomial, binomial, and trinomial form.
5) Divide radicals with monomial and binomial denominators. (Rationalize the denominator.)
6) Simplify radicals, which contain algebraic expressions.
7) Perform all of these proficiencies on radicals of higher order.

## Unit 5: Rational Algebraic Expressions and their Operations

Classes:
8
Project: Maintain file box on concepts learned.
Nat.Stan: \#1,3,5,6,7,8,9
Objective 1: The student will be able to display an understanding of the concept of rational expressions.

## Proficiencies:

1) Define numerator, denominator and vinculum.
2) Find the domain of a rational algebraic expression.
3) Find the GCF and LCM for rational algebraic expressions and display an understanding of their use with these expressions.

Objective 2: The student will be able to perform operations with rational algebraic expressions.

## Proficiencies:

1) Simplify rational algebraic expressions including members with negative exponents.
2) Add and subtract rational algebraic expressions with like and unlike denominators.
3) Multiply and divide rational algebraic expressions.
4) Simplify rational algebraic expressions with a combination of operations.
5) Simplify complex rational expressions.

## Unit 6: Exponential and Logarithmic Expressions

Classes: 8
Project: Maintain file box on concepts learned.
Tech: Video: Exponential and Logarithmic Functions ( 2 of the 610 min segments ) part 1: a matter of scale; part 2: calculating with logs Graphing calculator: use of the following keys: log, ln, etc.
Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to demonstrate an understanding of the relationship between exponential and logarithmic expressions.

## Proficiencies:

1) Define and use logarithm and antilogarithm.
2) Convert exponential to logarithmic expressions and vice versa.
3)Evaluate logarithmic expressions, i.e., and finding missing logs or antilogs.
3) Determine the domain of a logarithmic expression.
4) Write a logarithmic expression as a sum or difference of logs.
5) Write a logarithmic expression as a single log.
6) Know and use the change of base formula.
7) Find decimal approximation for logs.

## Unit 7: Functions and Relations

Classes: 7
Project: Maintain file box of concepts learned.
Tech: Graphing calculator: entering on the $\mathrm{y}=$ menu, setting the viewing window for the graph, determining domain and range, determining intervals of increase or decrease, determining $\mathrm{f}(\mathrm{x})$ is positive or negative, viewing translations and reflections, graphing the line of the average rate of change of a function over a given interval, viewing the vertical and horizontal line tests.
Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to demonstrate and understanding of relations and functions.

## Proficiencies:

1) Define a relation and a function.
2) Identify a relation and a function from the set of ordered pairs.
3) Identify the graph of a relation or function using the vertical line test.
4) Determine the domain and the range of a relation or a function from the set of ordered pairs or from the graph.
5) Identify and use function notation.
6) Determine the dependent and independent variable.

Objective 2: The student will be able to demonstrate an understanding of computations with functions and their graphs.

## Proficiencies:

1) Find the value of a function with a given domain.
2) Find the domain if the value of the function is given.
3) Find the sum, difference, product, quotient and composition of functions and determine the domain.
4) Determine the inverse of a function or relation and its domain and range.
5) Determine one to one correspondences using the horizontal line test.
6) Determine where a function is increasing or decreasing.
7) Identify the symmetry of the function as even and odd.
8) Identify vertical and horizontal translations of graphs of functions from their equations.
9) Identify compressions and stretches of graphs of functions from their equations.
10) Identify reflections of the graphs of functions over the axes from their equations.

## Unit 8: Equations and their Solutions

Classes: 15
Project: Maintain file box of concepts learned.
Tech: Video: Quadratics ( 610 min segments )

1) zeros and roots 2 ) factoring quad and graphs 3 ) completing the square and roots 4) quad formula and roots 5) complex roots 6) quad in real life.
Graphing calculator: using graph to determine $x$ intercepts as the root of equations, use the trace key, using the calc menu to find zeros, maximuns, minimuns, etc.
Nat.Stan: $\quad \# 1,3,4,5,6,7,8,9$
Objective 1: The student will be able to display an understanding of the concept of an algebraic equation.

## Proficiencies:

1) Determine the difference between simplifying and solving.
2) Determine the domain of the equation.
3) Determine the degree of the equation and its impact on the number of solutions.
4) Determine whether the roots or zeros of the equation are $x$ intercepts of the graph of the equation.
5) Use the properties of equality to transformation equations.
6) Display an understanding of equivalent equations.

Objective 2: The student will be able to find the roots of equations.

## Proficiencies:

1) Solve equations with one or two transformations.
2) Solve equations with like terms in one or both members.
3) Solve equations with distributive property.
4) Solve equations with fractions and decimals in the members.
5) Solve literal equations and formulas
6) Solve absolute value equations.
7) Solve equations containing squares or trinomial squares.
8) Solve quadratic equations by factoring, completing the square, and the quadratic formula.
9) Use the discriminant to determine the nature of the solutions.
10) Solve fractional equations and rational algebraic equations including members with higher degree polynomials.
11) Solve radical equations with one, two or more radicals in the numerator of denominator.
12) Determine extraneous solutions.
13) Solve selected higher degree polynomial equations.
14) Solve exponential equations.
15) Solve logarithmic equations.
16) Find inverse equations.

## Unit 9: Inequalities and their Solutions

Classes: 10
Project: Maintain file box of concepts learned.
Tech: Graphing calculator: viewing the solution to the inequality on viewing screen.
Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to display an understanding of the concept of the algebraic inequality.

## Proficiencies:

1) Know and use the word phrases with indicate an inequality, i.e., is at least; is at most; etc.
2) Determine the domain of an inequality.
3) Determine the degree of the inequality and its impact on the method of solution.
4) Use the properties of inequalities to transform the inequality.
5) Display an understanding of equivalent inequalities.
6) Know and use the concepts of intersection, union, conjunction, disjunction and their truth tables.

Objective 2: The student will be able to solve algebraic inequalities and write their solutions.

## Proficiencies:

1) Write an inequality from a number line graph.
2) Graph an inequality on the number line.
3) Determine the solutions of an inequality from a replacement set.
4) Solve inequalities with multiple transformations: i.e., like terms in one or both members; distributive property; containing fractions and decimals; etc.
5) Solve compound inequalities and absolute value inequalities.
6) Write these solutions in set notation.
7) Graph the solutions of these inequalities.
8) Solve quadratic inequality by factoring, quadratic formula and completing the square.
9) Solve polynomial and rational inequalities.

## Unit 10: Analytic Geometry

Classes: 25
Project: Maintain file box of concepts learned.
Tech: Video: Landscape of Geometry episode on range of change Graphing calculator: graph the following and setting the viewing window ( lines, absolute value, parabolas, cubic, quartic and higher degree, rational, radical, exponential \& logarithnic, etc.) , use graph to determine domain, range, asymptotes, and other significant critical features.
Objective 1: The student will be able to sketch the graph of relations and functions with their respective critical features.

## Proficiencies:

1) Sketch the graph of linear equations from all forms of the equation.
2) Determine the slope and intercepts.
3) Sketch the graph of parallel and perpendicular lines and determine the slope and the equation.
4) Sketch the graph of first degree absolute value and determine the slopes and the turning point.
5)Sketch the graph of the greatest integer function and determine its discontinuities
5) Sketch the graph of quadratic functions \& relations determining the vertex, intercepts, axis of symmetry, focus, directrix, minimum or maximum value and points of symmetry.
6) Sketch the graphs of rational functions determining the asymptotes, intercepts and points of discontinuity.
7) Classify discontinuities as removable or non-removable.
8) Sketch the graph of exponential and logarithmic functions, determining the intercept and asymptote.
9) Sketch the graphs of higher degree polynomial, determining the intercepts and minimum and maximum values.
10) Use the remainder theorem to determine zeros of the polynomial and points on the graph.
11) Determine the domain and range for the graphs of all functions and relations.

Objective 2: The student will demonstrate an understanding of the graphs of quadratic relations.

## Proficiencies:

1) Know and use the standard and general form of the equation for a circle.
2) Determine the center, focus and radius and use these to sketch the graph of the circle.
3) Know and use the standard and general form of the equation for an ellipse.
4) Determine the center, foci, vertices, and radii and use these to sketch the graph of the ellipse.
5) Know and use the standard and general form of the equation for the hyperbola.
6) Know and use the equation for the rectangular hyperbola.
7) Determine the center, foci, vertices, and asymptotes and use these to sketch of the hyperbola.
8) Know and use the standard, general and vertex form of the equation of quadratic relations.

Objective 3: The student will to able to recognize the families of functions.

## Proficiencies:

1) Recognize and sketch the parent graph of $|x|, x^{2}, x^{3}, \sqrt{ } x, a^{x}$, greatint. $x$.
2) Identify and perform horizontal \& vertical translations, dilations, and reflections over the $x$ and $y$ axes for these functions.

Objective 4: The student will be able to demonstrate an understanding of select formulas from geometry.

## Proficiencies:

1) Know and use the distance formula for horizontal and vertical line segments.
2) Know and use the distance formula for oblique line segments.
3) Know and use the formula for the distance between a point and a line.
4) Know and use the formula for finding the midpoint of a line segment

Objective 5: The student will be able to determine the equation of the function from the t chart.

## Proficiencies:

1) Recognize the add-add pattern of the linear function and determine its equation.
2) Recognize the add-multiply pattern of the exponential function and determine its equation.
3) Recognize the multiply-multiply pattern of the variation function and determine its equation.
4) Recognize the second differences pattern of the quadratic function and determine its equation.

## Unit 11: Systems

Classes: 10
Project: Maintain file box of concepts learned.
Tech: Graphing calculator: to view and find points of intersection
Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to demonstrate an understanding of a system of equations.

## Proficiencies:

1) Define a system of equations.
2) Determine the minimum and maximum number of possible solutions.
3) Determine the dimension of the system.
4) Know and use system vocabulary, i.e.; consistent, inconsistent, independent and dependent.

Objective 2: The student will be able to solve a system of equations and inequalities.

## Proficiencies:

1) Solve $2 X 2$ system of linear equations by graphing, substitution and linear combination.
2) Solve $3 X 3$ system of linear equations by linear combination.
3) Know and use determinants and Cramer's Rule to solve 2X2 and 3X3 systems of linear equations.
4) Solve nonlinear systems of equations by graphing, substitution and elimination.
5) Solve systems of linear inequalities by graphing.
6) Solve systems of nonlinear inequalities by graphing.

## Unit 12: Problem Solving

Classes: 25
Project: Maintain file box of concepts learned.
Presentation to class of verbal problem accompanied by some visual aid.
Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to demonstrate an ability to write and solve equations to solve work problems.

## Proficiencies:

1) Solve word problems with various themes using one or more variables; i.e., age, digits, consecutive values, dry/wet mixtures, uniform motion (wind, current, etc.), work, related rates, geometry, Pythagorean theorem, ratio, proportion, percent, etc.
2) Solve word problems, which generate a linear, quadratic or exponential equation.
3) Solve word problems, which generate a direct, inverse, joint or combined variation with integer and non-integer exponents.
4) Solve word problems, which generate a system of equations.

## Unit 13: Sequences and Series

Classes:
5
Project: Maintain file box of concepts learned
Tech: View the graph of sequences.
Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to demonstrate an understanding of a sequence.

## Proficiencies:

1) Write the first several terms of a sequence.
2) Write the terms of sequence defined by a recursion formula.
3) Find the sum of a sequence using summation notation. ( $\Sigma$ )
4) Determine if a sequence is arithmetic or geometric.

Objective 2: The student will demonstrate an ability to use the formulas for sequences and series.

## Proficiencies:

1) Know and use the formulas for finding a member of an arithmetic or geometric sequence.
2) Know and use the formulas for finding a partial sum of an arithmetic or geometric sequence.
3) Know and use the formula for finding the sum of an infinite geometric series.
4) Know Pascal's Triangle and the Binomial formula.
5) Know and use the Binomial Theorem to find the sum of a binomial raised to a whole number power.
6) Find missing members of a binomial expansion.

## ENRICHMENT UNITS:

## Unit 14: Combinatorics: Counting and Probability

Classes: 10
Project: Maintain file box of concepts learned.
Tech: Video: Probability ( 610 min segments )

1) uncertain certainty, 2) uniform probability model, 3) simple events
2) not so simple events, 5) probability distributions, 6) 6 Bernoulli Trails

Nat.Stan: \#1,3,4,5,6,7,8,9
Objective 1: The student will be able to demonstrate an understanding of the counting principles.

## Proficiencies:

1) Find all the subsets of a set.
2) Find the intersection and union of sets.
3) Find the complement of a set.
4) Know and use the two counting principles.

$$
\begin{aligned}
& n(A \text { and then } B)=n(A) \bullet n(B) \\
& n(A \text { or } B)=n(A)+n(B) \text { no elements in common } \\
& n(A \text { or } B)=n(A)+n(B)-n(A \cap B) \text { elements in common }
\end{aligned}
$$

Objective 2: The student will be able to demonstrate an understanding of the probability of an event.

## Proficiencies:

1) Define permutations and combinations.
2) Know and use factorial notation.
3) Solve counting problems by using permutations.

$$
P(n, r)=\frac{n!}{(n-r)!}
$$

4) Solve counting problems by using combinations.

$$
C(n, r)=\frac{n!}{(n-r)!r!}
$$

5) Count permutations with repetitions.
6) Use the additive rule to find probabilities of events with intersection and events that are mutually exclusive.
7) Compute probabilities of equally likely outcomes.

## Unit 15: Introduction to Trigonometry

Classes: 3
Project: Maintain file box of concepts learned.
Nat.Stan: \#1,2,3,4,5,6,7,8,9
Objective 1: The student will be able to recognize, evaluate and graph trigonometric expressions and equations.

## Proficiencies:

1) Recognize a periodic function.
2) Find the measurement of angles of rotation.
3) Define the six trigonometric functions, period, amplitude and phase shift.
4) Find the value of a trigonometric function.
5) Graph simple trigonometric functions.
6) Write equations of sinusoids from their graphs.
7) Know and use the definition of the inverse circular functions.
8) Evaluate inverse trigonometric expressions.

## Enrichment Objectives in Trigonometry

Objective 2: The student will be able to know and use the properties of trigonometric functions and to solve simple trigonometric equations.

## Proficiencies:

1) Know the reciprocal, quotient, and pythagorean properties.
2) Know and use the odd and even properties.
3) Know and use the cofunction properties for circular and trigonometric functions.
4) Know and use composite properties.
5) Know the multiple and half argument properties.
6) Solve simple trigonometric equations over a restricted domain and over the set of Reals.

Objective 3: The student will be able to solve triangle problems.

## Proficiencies:

1) Solve right triangles using trigonometric functions.
2) Know and use the Law of Cosines to solve oblique triangle problems.
3) Use the sine function to find the area of a triangle.
4) Use the Law of Sines to solve oblique triangle problems.
5) Recognize the ambiguous case in triangles.
